## Exercise 2

Verify inequalities (3), Sec. 4, involving Re z, Im z, and |z|.

## Solution

Inequalities (3) in Sec. 4 on page 9 are

$$\operatorname{Re} z \le |\operatorname{Re} z| \le |z| \quad \text{and} \quad \operatorname{Im} z \le |\operatorname{Im} z| \le |z|.$$
 (3)

Suppose z = x + iy. Then the first inequality becomes

$$x \le |x| \le \sqrt{x^2 + y^2},$$

which is true. The second inequality becomes

$$y \le |y| \le \sqrt{x^2 + y^2},$$

which is also true.